Computing Multiple Zeros of Polynomial Systems

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Given a polynomial system \$f\$ with a multiple zero \$x\$ whose Jacobian matrix at \$x\$ has corank one, we show how to compute the multiplicity structure of \$x\$ and the lower bound on the minimal distance between \$x\$ and other zeros of \$f\$.If \$x\$ is only given with limited accuracy, we give a numerical criterion for isolating a nearby cluster of \$\mu\$ zeros of \$f\$ (counting multiplicities) in a ball around \$x\$. Moreover, we also show how to compute verified and narrow error bounds such that a slightly perturbed system is guaranteed to possess an isolated corank one singular solution within computed error bounds. Finally, we present modified Newton iterations which converge quadratically if \$x\$ is close to an isolated exact singular solution of \$f\$. This is joint work with Zhiwei Hao, Wenrong Jiang, Nan Li.